

NAME: \_\_\_\_\_

Read all of the following information before starting the exam:

- **WRITE YOUR NAME AT THE TOP OF EACH PAGE** (you will lose points otherwise)
- **DO NOT WRITE ON THE FRONT OR BACK OF THE FIRST PAGE** other than writing your name.
- Show all work and give explanations where needed. I reserve the right to take off points if I cannot see how you arrived at your answer (even if your final answer is correct).
- Use only the paper provided, your one page notes and a pen or pencil.
- Write your answer in the box provided.
- This test has 5 problems. and is worth 70 points, It is your responsibility to make sure that you have all of the pages!
- Good luck!

1	
2	
3	
4	
5	
total	

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1. (20 points) Compute the following integrals:

(a)  $\int \tan^4(x) \sec^4(x) dx$

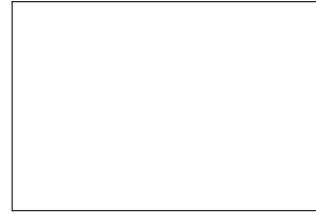


(b)  $\int \frac{dx}{(1+4x^2)^{\frac{3}{2}}}$

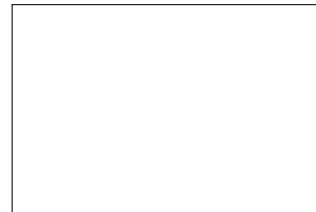


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(c)  $\int_{-1}^1 \frac{x+1}{-x^2-2x} dx$

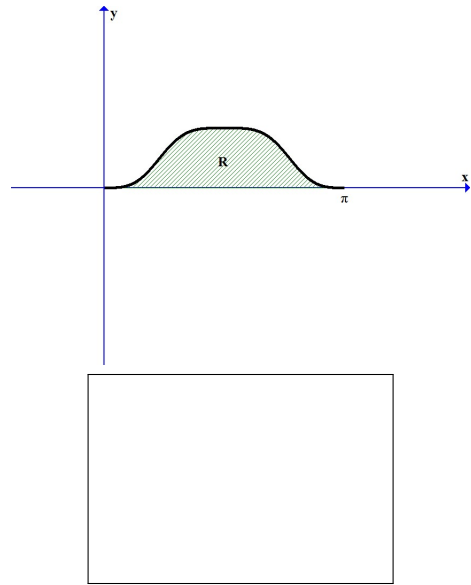


(d)  $\int \frac{4}{(x^2-1)(x+1)} dx$



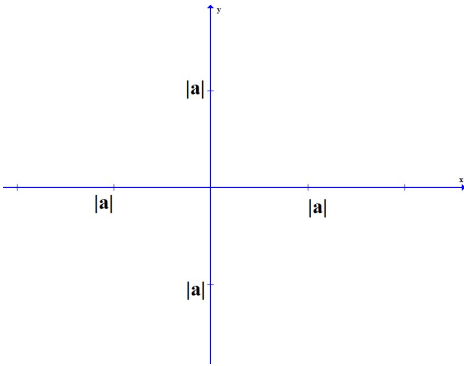
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**2.** (10 points) Let  $R$  be the region bounded by  $f(x) = \sin^3(x) \cos^2(x)$  the  $x$ -axis,  $x = 0$  and  $x = \pi$  (see picture below) set up the integral find the volume obtained by rotation  $R$  about the  $X$ -axis. Do not integrate.

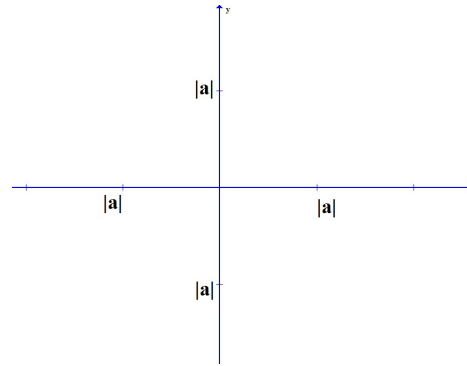


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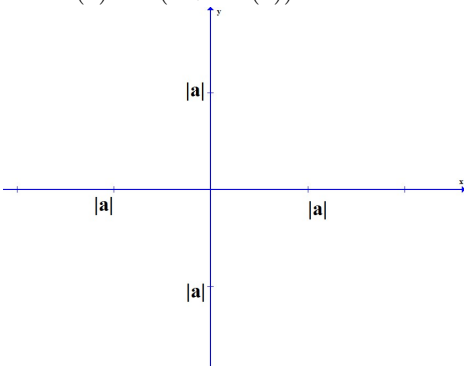
**3.** (20 points) Graph the following polar equations, then answer the question.



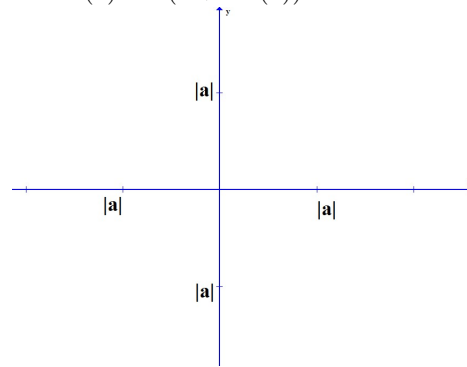
$$r(\theta) = a(1 + \cos(\theta)) \text{ for } a > 0$$



$$r(\theta) = a(1 + \cos(\theta)) \text{ for } a < 0$$



$$r(\theta) = 2a \cos(\theta) \text{ for } a > 0$$



$$r(\theta) = 2a \cos(\theta) \text{ for } a > 0$$

Find the area between  $r_1(\theta) = 2 \cos(\theta)$  and  $r_2(\theta) = -2(1 + \cos(\theta))$ . Be careful with the limits of integration, the curves have a different periods (they finish their cycles at different  $\theta$ 's.)

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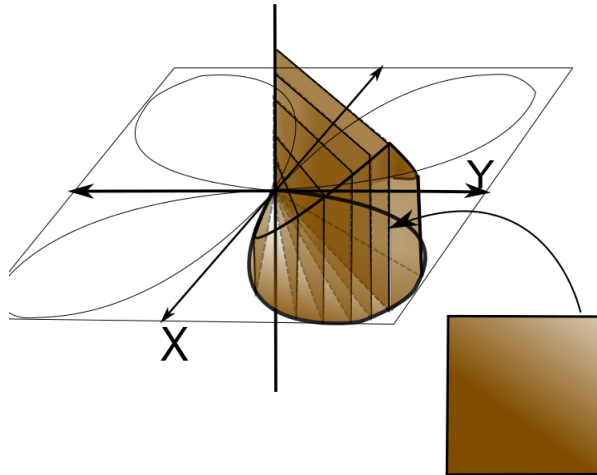
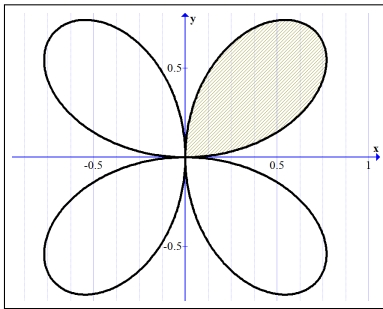
**4.** (10 points)

Let  $A$  be the 2 dimensional region enclosed by the polar equation  $r(\theta) = \sin(2\theta)$  for  $0 \leq \theta \leq \frac{\pi}{2}$  and  $V$  be the solid with base  $A$  whose cross sections are squares perpendicular to the base which radiate outwards from the center to the edge of the shape (see picture below.)

(a) Find the function  $f(\theta)$  so that the volume of  $V$  is given by  $\int_0^{\frac{\pi}{2}} f(\theta) d\theta$   
(hint: the estimating shape is not a square prism.)

(b) Find the volume of  $V$  i.e. evaluate  $\int_0^{\frac{\pi}{2}} f(\theta) d\theta$ .

(c) Let  $B$  was the 2 dimensional region enclosed by  $r(\theta) = \sin(2\theta)$  for  $0 \leq \theta \leq 2\pi$  and  $W$  the solid with base  $B$  whose cross sections are squares perpendicular to the base which radiate outwards from the center to the edge of the shape. Then is the volume of  $W$  given by  $\int_0^{2\pi} f(\theta) d\theta$  where  $f(\theta)$  is the function you found in part (a)



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**5.** (10 points) Choose either problem 1 or 2 but not both, make it clear which problem you choose.

1. (a) Give the parametric equation (in terms of  $t$ ) for a circle of radius one oriented in the counter-clockwise direction which finishes a full cycle on the interval  $0 \leq t \leq 2\pi$ .
- (b) Give a parametric equation for a line segment between the points  $(3, 2)$  and  $(5, 1)$  make sure to include the interval for  $t$
- (c) Give the equation (in terms of  $x$  and  $y$ ) of the tangent line to the parametric curve  $x(t) = \sin(2t)$ ,  $y(t) = 2 \sin(t)$  at the point  $(\frac{\sqrt{3}}{2}, 1)$ .

2. Compute the following integral

$$\int_{-\pi}^{\pi} x \sin^2(2x) \cos(2x) dx$$