## Homework 5: Chapter 3

Reading: Chapter 3 pgs 17-20, Appendix A pgs 195-198
Exercises:

1. From the book: 3.1, 3.2, and 3.4
2. Use the following example to show that sequential comparison fails the unanimity criterion, with candidates ordered alphabetically:

| 1 | 1 | 1 |
| :---: | :---: | :---: |
| $A$ | $C$ | $B$ |
| $B$ | $A$ | $D$ |
| $D$ | $B$ | $C$ |
| $C$ | $D$ | $A$ |

3. Our solution to Exercise (2.5) from class happens to also show that pairwise comparison admits losing spoilers. I'll recall the example here:

| 1 | 1 |
| :---: | :---: |
| $X$ | $Z$ |
| $Y$ | $X$ |
| $Z$ | $Y$ |

Show that there is a losing spoiler for ALL POSSIBLE examples satisfying the conditions in Exercise (2.5), as long as $n=3$. (Hint below)
Bonus round: (optional) construct an example with $n=4$ which satisfies the conditions of Exercise \#2.5, but doesn't have any spoilers.
4. Prove that if there is a Majority candidate, there will not be any spoilers for plurality.
5. Prove that if there is a Condorcet candidate, then there will not be any spoilers for pairwise comparison. Complete Exercise (3.4) to notice that Condorcet candidates can be spoilers for plurality.

Book solutions.
Other solutions (in progress-ish)

Hint to Exercise 2: Draw the comparison graph for the example in class. Can you draw it for any example with $n=3$ under the conditions of Exercise 2.5?

Now, consider an election with any number of $n$ candidates. Consider the comparison graph. If you remove one candidate, how does the new comparison graph change?

