## Homework 16: Chapter 16

Reading: Chapter 16
Book Exercises: 16.2 (Solutions)
Other Exercises: (Solutions)

1. Suppose avid pie-eaters $A$ and $B$ are dividing a homogeneous pie with pumpkin and Boston creme components.
(a) If $A$ likes pumpkin three times as much as Boston creme, describe $A$ 's ideal pie ie, what proportions of the whole would $A$ like each component to be?
(b) If $B$ likes Boston creme four times as much as pumpkin, describe $B$ 's ideal pie. (you might want to put this information in a table)
(c) Consider these two cuts:

|  | $S_{1}$ | $S_{2}$ |
| :---: | :---: | :---: |
| Pump | $1 / 3$ | $2 / 3$ |
| BosCr | 1 | 0 |


|  | $T_{1}$ | $T_{2}$ |
| :---: | :---: | :---: |
| Pump | $5 / 6$ | $1 / 6$ |
| BosCr | 0 | 1 |

Remember: the cut on the left is $1 / 3$ pumpkin and all the Boston creme in the first slice, $S_{1}$, and the rest in $S_{2}$. For the cut on the right, $T_{1}$ has $5 / 6$ pumpkin and none of the Boston creme.
Which cut(s) would $A$ make to guarantee getting $A$ 's fair share?
(d) If $A$ makes a good cut for playing I cut you choose using one of the cuts above, which slice would $B$ pick?
(e) There are many cuts that $A$ could make to guarantee getting $A$ 's fair share in I cut you choose. Can you find others?

